



# MEMORY AID TIPS 2.5

Greatest Integer Function  
Parameters “a” & “b”

Parameters		Geometric Transformations	Important Additional Information
a	If $ a  > 1$	Vertical Stretch	<ul style="list-style-type: none"> <li>The value of <math> a </math> determines the vertical distance between each step</li> <li>If the value of <math> a </math> is a number other than 1 and it is negative, there are 2 geometric transformations</li> </ul>
	If $0 <  a  < 1$	Vertical Shrink	
	If $a < 0$	Reflection off x - axis	
b	If $ b  > 1$	Horizontal Shrink	<ul style="list-style-type: none"> <li>The horizontal length of each step is <math> 1/b </math></li> <li>If the value of <math> b </math> is a number other than 1 and it is negative, there are 2 geometric transformations</li> </ul>
	If $0 <  b  < 1$	Horizontal Stretch	
	If $b < 0$	Reflection off y - axis	



②

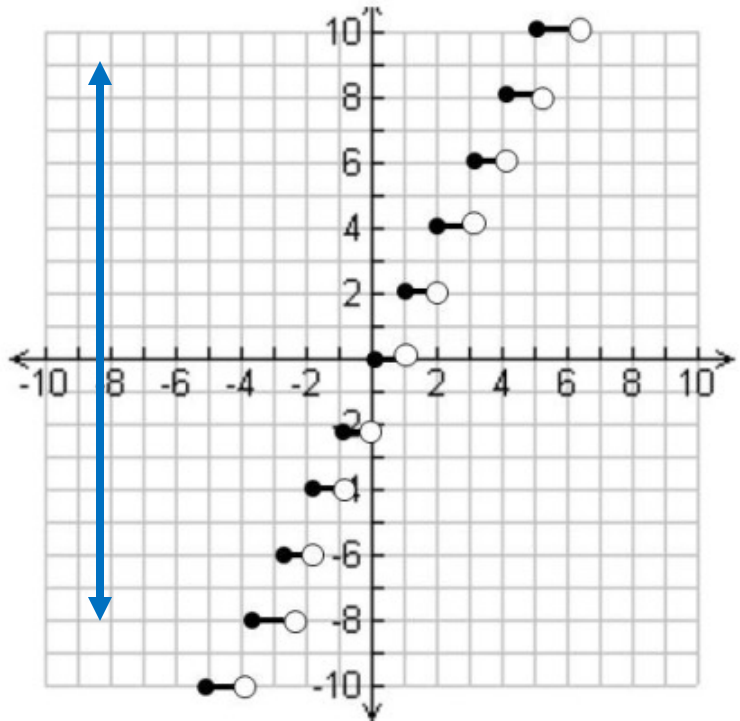
When  $a > 1$

①

$$y = 2[x]$$

$$a = 2 \quad b = 1$$
$$h = 0 \quad k = 0$$

③



④

x	y
$[0, 1[$	0
$[1, 2[$	2
$[2, 3[$	4
$[3, 4[$	6
.....	....

⑤ The geometric transformation of this function is:

Vertical stretch.

- Length of steps = 1
- Vertical distance between each step = 2
- Steps are going up

②

When  $0 < a < 1$

①

$$y = \underline{0.5} [x]$$

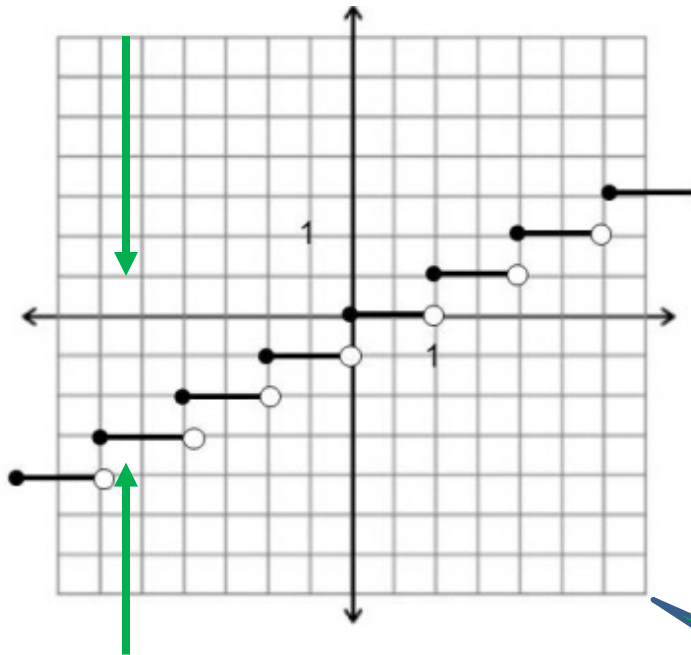
$a = 0.5$

$b = 1$

$h = 0$

$k = 0$

③



④

x	y
$[0, 1[$	0
$[1, 2[$	0.5
$[2, 3[$	1
$[3, 4[$	1.5
.....	....

⑤

The geometric transformation of this function is:

vertical shrink

- Length of steps = 1
- Vertical distance between each step = 0.5
- Steps are going up

②

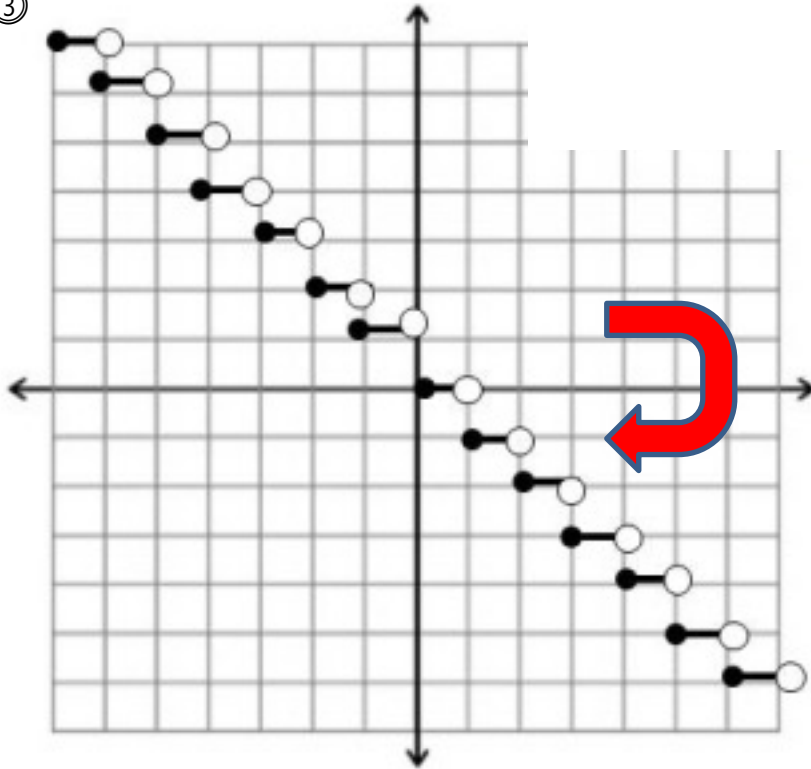
①

$$y = \underline{-1} [x]$$

When  $a < 0$

$$\begin{aligned} a &= -1 & b &= 1 \\ h &= 0 & k &= 0 \end{aligned}$$

③



④

x	y
$[-2, -1[$	2
$[-1, 0[$	1
$[0, 1[$	0
$[1, 2[$	-1
.....	....

- Length of steps = 1
- Vertical distance between each step = 1
- Steps are going down

⑤

**The geometric transformation of this function is:**

Reflection off the x axis

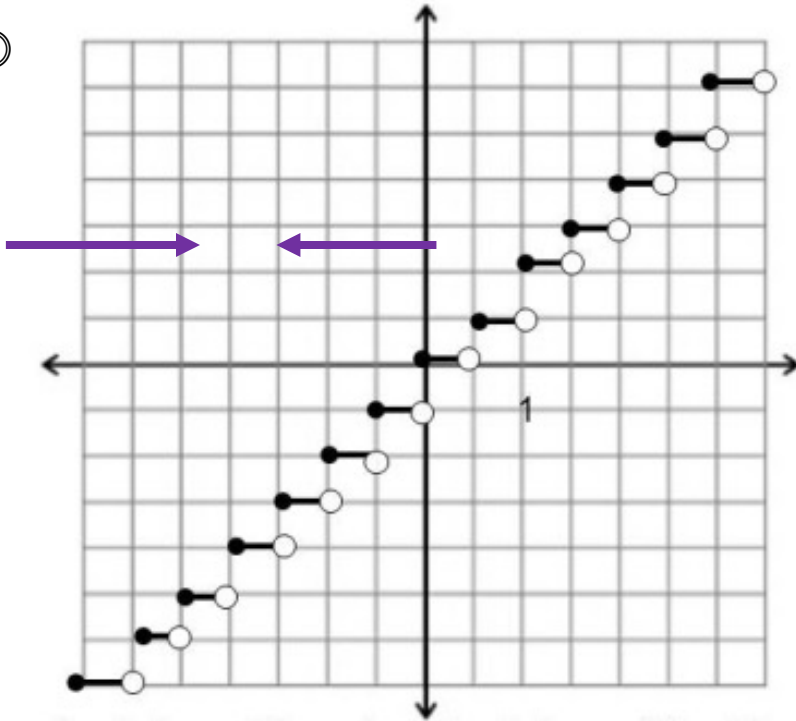
②

①  $y = \left[ \frac{2}{1} x \right]$

When  $b > 1$

$a = 1$       $b = 2$   
 $h = 0$       $k = 0$

③



④

x	y
$[-1, -0.5[$	-2
$[-0.5, 0[$	-1
$[0, 0.5[$	0
$[0.5, 1[$	1
.....	....

- Length of steps =  $0.5 = |1/b|$
- Vertical distance between each step = 1
- Steps are going up

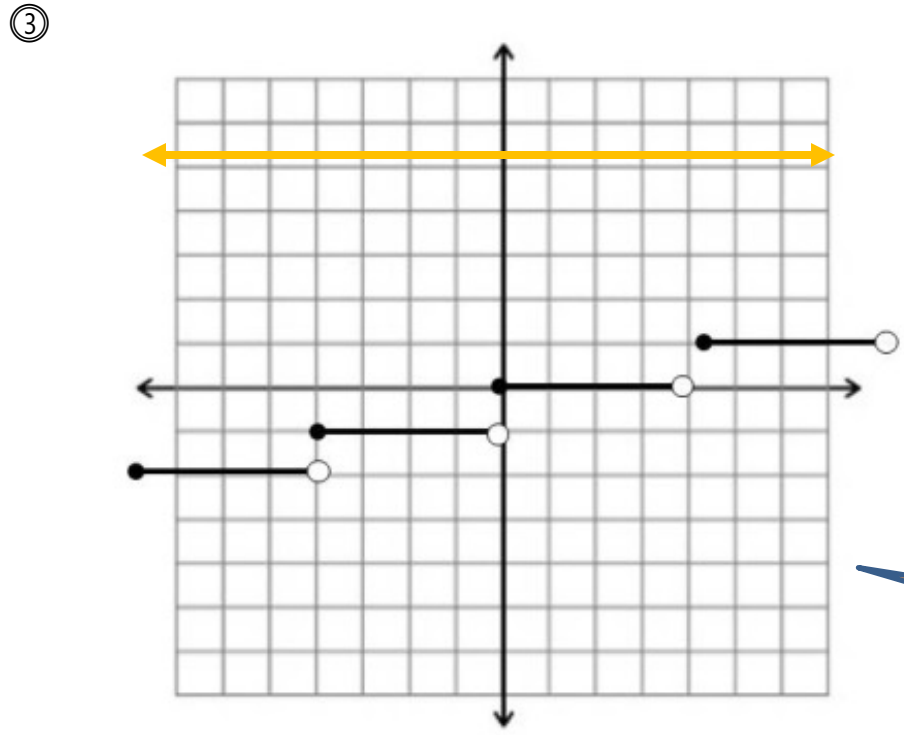
⑤

The geometric transformation of this function is:  
horizontal shrink

When  $0 < b < 1$

①  $y = \left[ \frac{0.25}{\quad} x \right]$

②  $a = 1$       $b = 0.25$   
 $h = 0$       $k = 0$



④

x	y
$[-8, -4[$	-2
$[-4, 0[$	-1
$[0, 4[$	0
$[4, 8[$	1
...	...

- Length of steps =  $|1/b| = |1/0.25| = 4$
- Vertical distance between each step = 1
- Steps are going up

⑤ The geometric transformation of this function

horizontal stretch

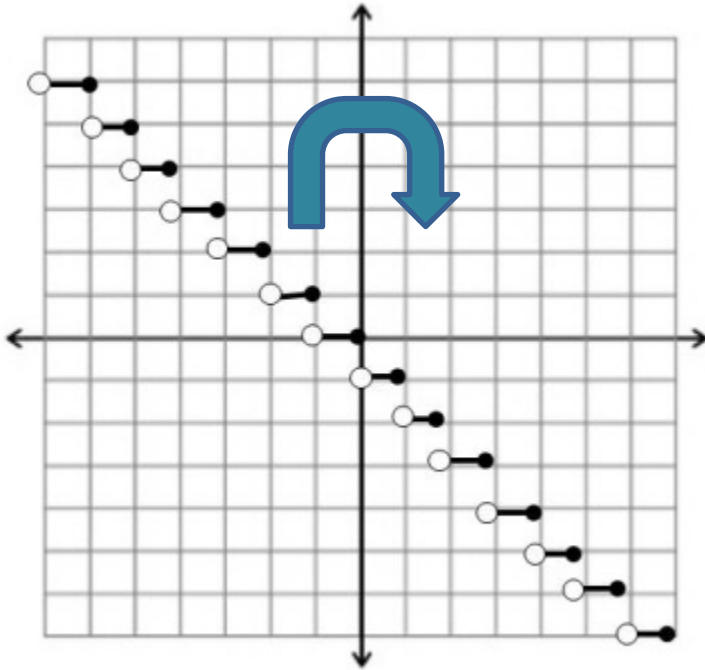
②

① 
$$y = \left[ \frac{-}{\quad} x \right]$$

When  $b < 0$ 

$$\begin{array}{ll} a = 1 & b = -1 \\ h = 0 & k = 0 \end{array}$$

③



④

x	y
$] -2, -1]$	1
$] -1, 0]$	0
$] 0, 1]$	-1
$] 1, 2]$	-2
.....	....

⑤

**The geometric transformation of this function is:**

reflection of the y axis

- Length of steps = 1 =  $|1/b|$
- Vertical distance between each step = 1
- Steps are going down



$$f(x) = a[bx]$$

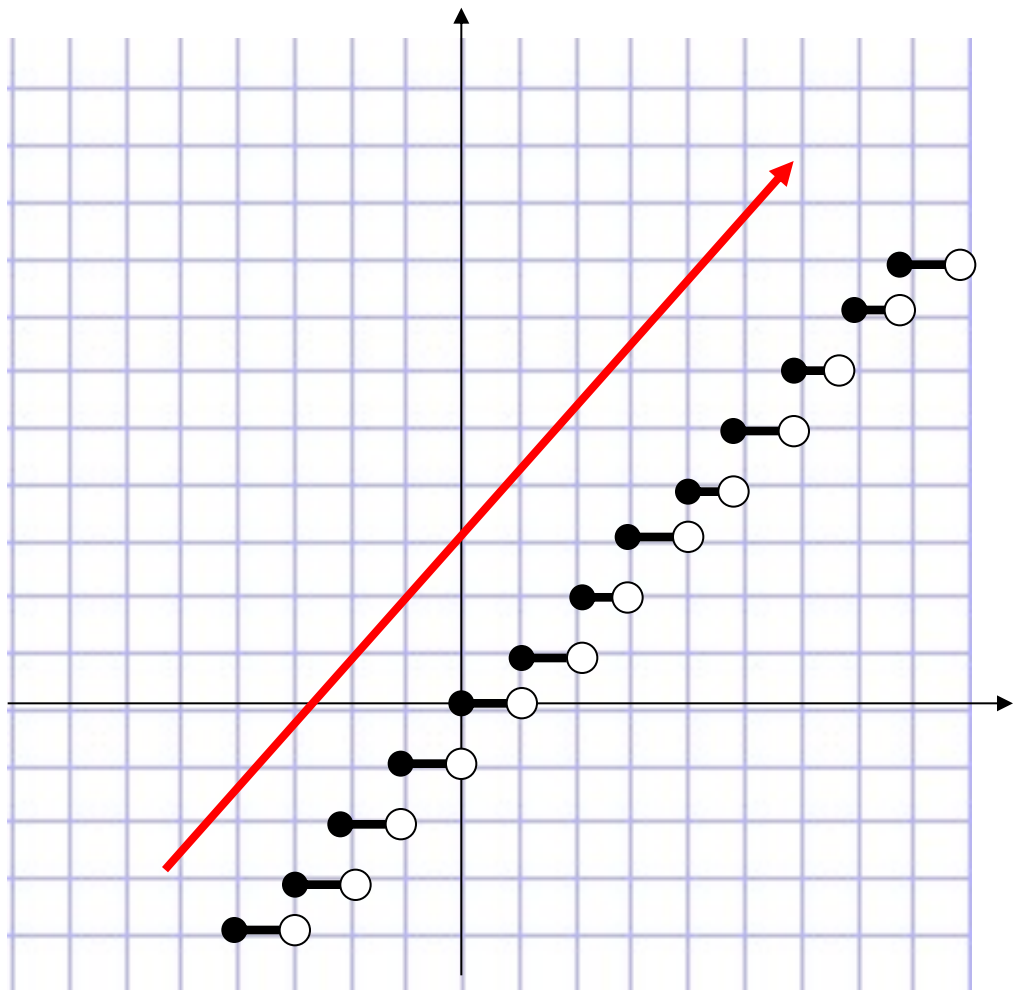
$$a > 0$$

$$b > 0$$



$$+ \quad x \quad + \quad = \quad +$$

$a \bullet b = \textit{positive slope}$



$$f(x) = a[bx]$$

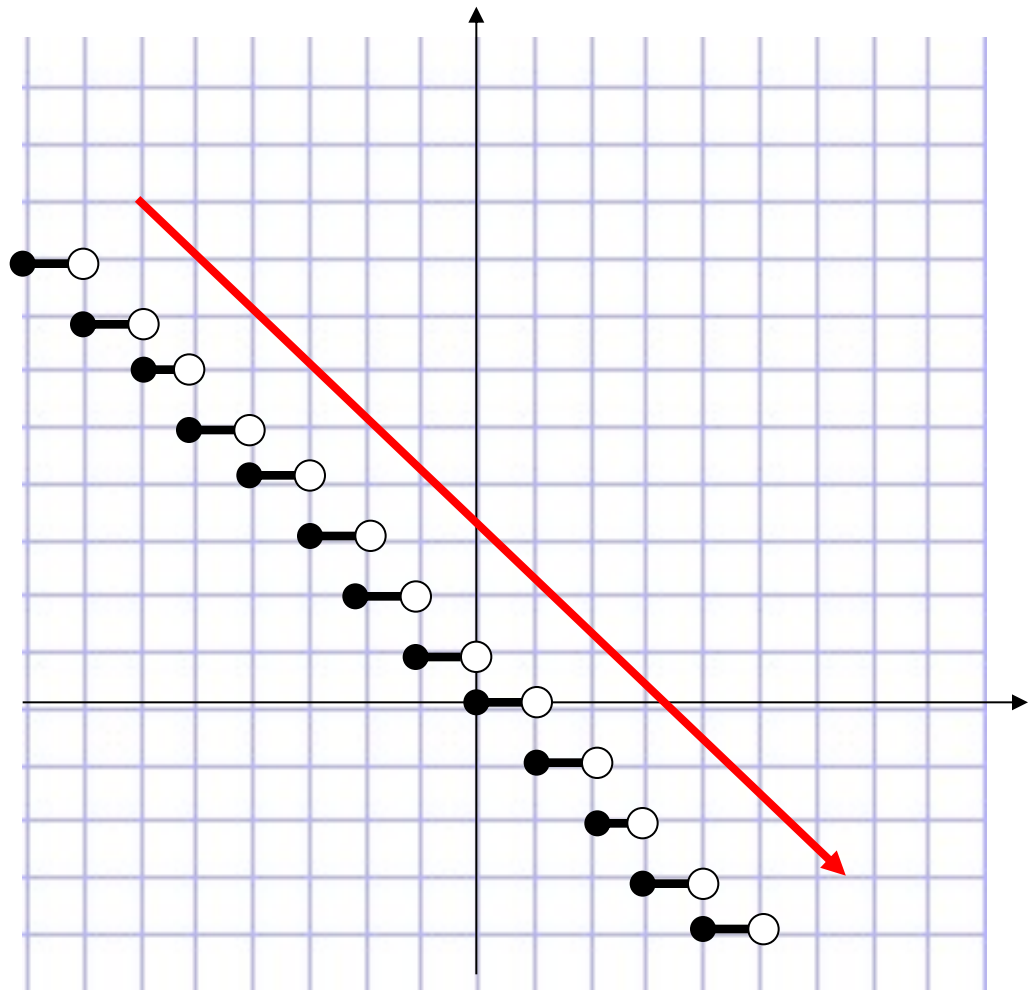
$$a < 0$$

$$b > 0$$



$$- \quad x \quad + \quad = \quad -$$

$a \bullet b = \textit{negative slope}$



$$f(x) = a[bx]$$

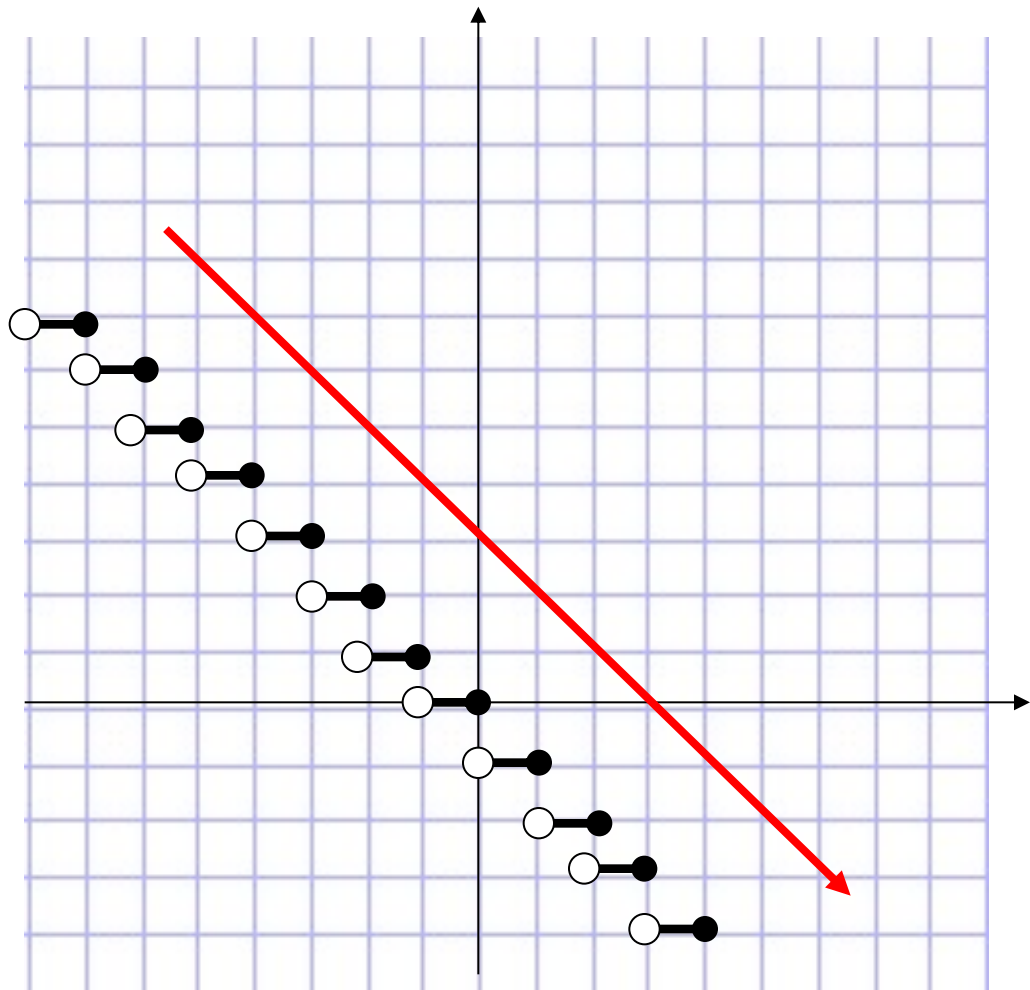
$$a > 0$$

$$b < 0$$



$$+ \quad x \quad - \quad = \quad -$$

$a \bullet b = \textit{negative slope}$



$$f(x) = a[bx]$$

$$a < 0$$

$$b < 0$$



$$- \quad x \quad - \quad = \quad +$$

$a \bullet b = \text{positive slope}$

